Terrain Modeling and Soil Erosion Simulation Final Report

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Contents:

<u>1. General aspects of modeling and GIS</u>

 <u>1.1 Simulation and modeling</u>
 <u>1.2 Types of models</u>

 <u>2. Erosion models and types of erosion processes</u>

 <u>2.1. Exponents in RUSLE3d</u>
 <u>2.2 Exponents in USPED</u>

 <u>3. Implementation in ArcGIS8.1</u>
 <u>4. On-line tutorial</u>
 <u>5. Fort Hood application</u>

 <u>5.1 Comparison with NRCS erosion inventory</u>
 <u>5.2 Planning prevention measures with GIS</u>

 <u>Conclusions</u>

 <u>References</u>

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1. General aspects of modeling and GIS

One of the key challenges in environmental research is to model interacting physical processes with sufficient accuracy and efficiency. Rapid development of computer technology offers new opportunities to tackle extremely complex environmental problems. Computational approaches belong to "young" methodologies which were developed only over the past few decades and as such, they have their own rules, challenges, successes and limitations. The role of algorithms, data structures, computationally efficient methods, advanced visualization and exploration of parallelism are crucial for new advances in environmental research and require close collaboration between traditional research disciplines and computational science.

Originally, GIS applications were focused on static spatial data processing, analysis and computer cartography. However, development of new mapping technologies and computer capabilities together with acute environmental problems have pushed the GIS applications into more sophisticated levels. Advanced geoscientific applications involve modeling landscape processes at an unprecedented level of detail. Nevertheless, the process-based modeling of geospatial phenomena involves substantially more uncertainty than modeling in physics or chemistry because of the above mentioned complexity. Practical solutions have to rely, then, on the best possible combination of physical models, empirical evidence, intuition and available measured data. In physics, accuracy is usually understood in a much stricter sense, because many fundamental laws are known over a broad range of scales in energy, distance or time. For example, the Schrodinger equation describes matter at the electronic level virtually exactly, that means, within spectroscopic accuracy of 6 to 12 digits. This is seldom the case in complex geoscientific applications can be in many instances considered satisfactory.

1.1 Simulation and modeling

Computational approaches to investigations of physical systems are based on simulation and modeling. By **simulation** we mean a computer representation of reality in which the simulated system is governed by a set of known physical laws expressed in mathematical language. In this case the model is already in place and its range of validity and accuracy is supposed to be well-known and verified. The task of simulation is to solve it for a particular realistic situation. The fact that the fundamental laws are known does not mean that simulations are straightforward or easy. The corresponding equations are often difficult to solve and barriers in computational feasibility and efficiency often limit accuracy, resolution or size of the modeled system.

On the other hand, by **modeling** we mean a process by which the scientist is trying to build a simplified version of reality for a phenomenon for which the fundamental laws are either unknown, impractical to use or simply do not exist. This typically involves systems which are very complex, with many constituents and a variety of interactions between them and with limited amount of available experimental information. Typical examples are many ecological models, and systems which involve anthropogenic activities. The modeling process often involves trial and error and in some cases its predictive power, accuracy and relation to reality may be a research problem on its own.

1.2 Types of models

Physical systems are often described by a combination of deterministic (physically based) and empirical (observation based) models. **Empirical models** are based on observations and statistical analysis of observed data and their applicability is limited to the conditions for which they were developed. They can provide a rough picture of the phenomenon under study, but they cannot explain how the system works. Because of their simplicity, they are widely used for practical applications and as components of more complex models for the sub-processes for which the physical model is unknown or too complicated.

Current research and development in physical systems modeling is focused on **distributed, process-based models,** often dynamic in three dimensional (3D) space. This trend has been stimulated by the availability of geospatial data and supporting geographic information system (GIS) tools. GIS has greatly reduced the time for preparation of inputs, however, this task can still be rather tedious and time consuming. Artifacts from interpolation remain a perennial problem and the support for high precision floating point, temporal and multidimensional data is still inadequate. Therefore coupling of GIS and models is done at various levels and incorporation of GIS functionality within the modeling systems is now quite common. The models of physical processes are often core modules for integrated modeling systems, due to their impact on ecosystems and society. Models of physical systems are also important components of decision support systems.

2. Erosion models and types of erosion processes

A typical example of modeling of a complex landscape process which requires combination of empirical and physics-based methods is soil erosion, and sediment transport and deposition modeling. This combination is necessary because there are still gaps in understanding of the relevant processes. Also, some of the processes are too complex or require difficult to measure parameters to be incorporated using the known physics principles.

A number of erosion models explicitly distinguish and simulate various types of erosion processes, such as sheet erosion, rills, gullies etc. However such an approach requires a large number of empirical input parameters which cannot be obtained at sufficient accuracy for landscape scale applications without substantial cost. Therefore in simpler models, the different impact of these various processes is averaged and incorporated through empirical parameters, which is the case for RUSLE3d and USPED models. These two models and their various applications have been covered in previous reports and publications (Mitasova et al. 1995-2000) and in the Landscape Erosion Modeling Tutorial. Here we provide some explanations regarding the types of erosion modeled and selection of parameters (Engel, Desmet and Govers).

Both models replace slope length by upslope area as a measure of water flow. This makes the models applicable to complex topography. It also means that the model captures impact of a wider range of types of flow than the original USLE. It includes the combined, averaged impact of sheet and rill flow on hillslopes as well as concentrated flow erosion and potential for gully formation that has not been covered by traditional USLE. While the sheet and rill flow rates are comparable to USLE for the range of slopes and hillslope length typical for USLE applications (see Wilson and Moore 1992) erosion rate estimates for concentrated flow erosion and very long hillslopes are not sufficiently verified because of lack of empirical data. However, preliminary comparisons show that the models correctly predict over one to two magnitudes of increase in erosion rates due to concentrated flow and these areas should be classified as areas of high erosion risk (rather than excluded from the results). When making erosion risk assessment using RUSLE3d and USPED it is therefore not necessary to add impact of gullies from field observations because they are already incorporated.

2.1. Exponents in RUSLE3d

The basic equation for RUSLE estimates erosion rate by multiplying the following empirical factors:

$$E = R K L S C P$$

where E is the average soil loss, R is the rainfall intensity, K is the soil, C is the cover, P is the prevention practices and LS is the topographic factor:

$$LS(\mathbf{r}) = (m+1) [A(\mathbf{r}) / a_0]^m [\sin b(\mathbf{r}) / b_0]^n$$

where *A* is upslope contributing area per unit contour width, *b* is the slope, $a_0 = 22.1m$, $b_0 = 0.09$, *m* is 0.4-0.6 and n=1-1.3. Exponents for water and slope terms in the sediment transport and detachment equations reflect the interaction between different types of flow and soil detachment and transport. We explain their application and impact on the result in the following sections.

For *sheet flow*, detachment and sediment transport increases relatively slowly with the amount of water. Geometric properties of topography (slope, curvatures) play a more important role in the evolution of the pattern of soil detachment and net erosion/deposition than the pattern of water flow. This type of flow is typical for areas with good vegetation cover but also for a severely compacted, smooth soil cover where compaction prevents soil detachment and formation of rills. This type of flow is reflected by the lower value of exponent *m* for the water term represented by the upslope area (Figure 1. Click on the images to get full size figures).



Figure. 1 RUSLE3D LS factor for prevailing sheet flow reflected by the value of m=0.1. In this case the impact of steeper slope on the erosion pattern is stronger than the impact of concentrated flow.

SUM = 334314	
Number of cells: 735318	
Minimum: O	
Maximum: 3.1872103214	
Range: 3.18721	
Arithmetic Mean: 0.454652	
Variance: 0.137468	
Standard deviation: 0.370766	
 MAP: 1.1*exp(house3.dsd*3./22.13,0.1)*exp(sin(sl3.rst50s2)/0 	.0896,1.3)
Category Information	olo
# description	cover
acres	
 0-1 stable	
1-5 low 157.96604	9.62

* no_data	 	 	0.47
7.64897			

If both types of flow are present in the given area, which is usually the case due to spatial variability in land cover and soil properties, the value m=1.4 provides reasonable, averaged results (Figure 2). It has also a theoretical foundation (Moore and Burch 1986) and is being used, for example, by Engel (1999) This exponent balances the impact of turbulent and sheet overland flow.



Figure 2. RUSLE3D LS factor for averaged sheet, rill, and gully erosion including both impact of concentrated flow and slope pattern using m=0.4.

MAP: 1.4*exp(house3.dsd*3./22.13,0.4)*exp(sin(sl3.rst50s2)/0.0896,1.3) _____ ____| Category Information 8 #|description | cover| acres _____ |----___| 68.45 | 1123.70468 | 1-5|low....| 30.77| 505.07843 4.51560 0.75779 7.64897 _____ |---------|

For prevailing *rill and gully erosion* that appears on disturbed land, with soils vulnerable to rilling and gully formation, creating conditions for highly turbulent water flow, the impact of the water term is much higher, reflected by the higher exponent *m*.



Figure 3. RUSLE3D LS factor for prevailing rill and gully erosion reflected by the value of m=0.6. In this case the impact of flow on the erosion pattern is stronger than the impact of slope and overall erosion rates are much higher.

```
SUM = 1112308
Number of cells: 735318
Minimum: 0
Maximum: 120.2604675293
Range: 120.26
Arithmetic Mean: 1.51269
Variance: 5.92545
Standard deviation: 2.43422
----|
MAP: 1.6*exp(house3.dsd*3./22.13,0.6)*exp(sin(sl3.rst50s2)/0.0896,1.3)
_____
----|
       Category Information
                     8
  # description
                     cover
acres
----|
 853.10417
 719.65615
 51.25830
9.30009
0.73779
 7.64897
   _____
|-----
----|
```

If we assume that a dense vegetation cover prevents creation of rills and keeps water flow in dispersed, sheet flow while the loose, bare soil has an opposite impact, increasing the flow turbulence and formation of rills, we can use a spatially variable exponent based on the cover. In the following example, we have used the exponents m=0.2 for forest, m=0.4 for grass, m=0.5 for dormant sparse grass and m=0.6 for disturbed areas. The result increases the negative impact of disturbed areas and reduces the impact of vegetated areas.



Figure 4. RUSLE3D LS for variable m exponent

```
SUM = 792530.019225
Number of cells: 735318
Minimum: 0
Maximum: 86.2473754883
Range: 86.2474
Arithmetic Mean: 1.07781
Variance: 1.7033
Standard deviation: 1.30511
----|
MAP:
(1.0+mvar)*exp(house3.dsd*3./22.13,mvar)*exp(sin(sl3.rst50s2)/0.089...
(
       _____
|--
____|
        Category Information
                          00
   #|description
                          | cover|
acres
        _____
|----
----|
62.89 | 1032.51487 |
581.81698
17.44907
2.22891
0.04667
```

* no	data.	 	 	 	0.47
7.64897					

Note, that RUSLE3d provides a variable m exponent expressed as a function of slope angle, which reflects the fact that planar hillslopes with low slope have prevailing dispersed flow, while flow on steeper slopes can be more turbulent. However, this exponent gives reasonable results only for shorter slopes. For slopes hundreds of meters long, or for concentrated flow, this exponent predicts extremely high values of erosion rates.

When different LS factors are used in the full RUSLE3D equation, the quantitative results and pattern are as follows:



Figure 5. Full RUSLE3D estimate with a) constant m=0.4; b) variable m. The result with variable m predicts higher risk for gullies.

m=0.4 SUM = -6377646 Number of cells: 722067 Minimum: -734.1213378906 Maximum: -0 Range: 734.121 Arithmetic Mean: -8.83249 Variance: 328.88

```
Standard deviation: 18.135
m=variable
SUM = -9074719
Number of cells: 722067
Minimum: -3863.8823242188
Maximum: -0
Range: 3863.88
Arithmetic Mean: -12.5677
Variance: 1269.59
Standard deviation: 35.6313
```

2.2 Exponents in USPED

USPED (Unit Stream Power - based Erosion Deposition) is a simple model that predicts the spatial distribution of erosion and deposition rates for a steady state overland flow with uniform rainfall excess conditions. It assumes that the erosion process is transport capacity limited. The model is based on the theory originally outlined by Moore and Burch (1986) with numerous improvements. For the transport capacity limited case, we assume that the sediment flow rate $q_s(\mathbf{r})$ is at the sediment transport capacity $T(\mathbf{r})$, $\mathbf{r}=(x,y)$ which is approximated by (Julien and Simons 1985)

 $|\mathbf{q}_{s}(\mathbf{r})| = T(\mathbf{r}) = K_{t}(\mathbf{r}) |\mathbf{q}(\mathbf{r})|^{m} \sin b(\mathbf{r})^{n}$

where $b(\mathbf{r})$ [deg] is slope, $\mathbf{q}(\mathbf{r})$ is water flow rate, $Kt(\mathbf{r})$ is transportability coefficient, which is dependent on soil and cover; *m*, *n* are constants that vary according to type of flow and soil properties. For overland flow the constants are usually set to m=1.6, n=1.3(Foster 1993). Steady state water flow can be expressed as a function of upslope contributing area per unit contour width $A(\mathbf{r})[m]$

$$|\mathbf{q}(\mathbf{r})| = A(\mathbf{r}) i$$

where i[m] is uniform rainfall intensity (note: approximation by upslope area neglects the change in flow velocity due to cover). No experimental work was performed to develop parameters needed for USPED, therefore we use the USLE or RUSLE parameters to incorporate the approximate impact of soil and cover and obtain at least a relative estimate of net erosion and deposition. We assume that we can estimate sediment flow at sediment transport capacity as:

$$T = R K C P A^m (\sin b)^n$$

where $R \sim i^m$, *KCP*~*Kt* and *LS*= $A^m \sin b^n$, and *m*=1.0-1.6, *n*=1.0-1.3 Then the net erosion/deposition is estimated as a change in sediment flow rate expressed by a divergence in sediment flow:

$$ED = \operatorname{div} (T \cdot \mathbf{s}) = \operatorname{d}(T^* \cos a)/\operatorname{dx} + \operatorname{d}(T^* \sin a)/\operatorname{dy}$$

where a [deg] is aspect of the elevation surface (or direction of flow, steepest slope direction, minus gradient direction).

Because USPED computes divergence of sediment flow, the impact of the exponents is more complex. The water flow term exponent here controls the ratio between the extent of erosion and deposition as it is illustrated by the following examples. It reflects the fact that turbulent flow can carry sediment farther and the impact of concentrated erosion will be wider than if flow is dispersed by vegetation. The following figures (Figures 6, 7, 8,9,10) demonstrate the influence of the exponent *m* on the erosion/deposition pattern and gully erosion risk estimates.



Figure 6. Spatial pattern of topographic potential for erosion and deposition by USPED with m=1, prevailing dispersed sheet flow, deposition extends high onto hillslopes.



Figure 7. Spatial pattern of topographic potential for erosion and deposition by USPED with m=1.4, both sheet flow and rill flow influence erosion and deposition. Deposition starts lower on the hillslope, gullies start farther towards the headwater area and they are wider.



Figure 8. Spatial pattern of topographic potential for erosion and deposition by USPED with m=1.6, with prevailing rill and concentrated flow. Extent of deposition is further

reduced and the potential for gullies starts very high in the headwater area, so gullies are even longer and wider.



Figure 9. Spatial pattern of topographic potential for erosion and deposition by USPED with variable m.



Figure 10. Full USPED with variable m

3. Implementation in ArcGIS8.1

The RUSLE3d and USPED models as described above were implemented in ArcGIS 8.1 as well as in ArcView3.x and GRASS GIS. For ArcView, still the most widely used GIS on installations, we developed sample Avenue scripts to make it easier to run the models. We examined implementation in ArcGIS 8 using the ArcModel interface, but that interface was not released with ArcGIS 8.1 and is reportedly undergoing major revision with no release date set. Detailed procedures for running both models in ArcGIS are provided in the on-line tutorial developed as part of this work (see link below).

4. On-line tutorial

Using Soil Erosion Modeling for Improved Conservation Planning: A GIS-based Tutorial (http://www.gis.uiuc.edu/erosion) is a richly illustrated hypertext tutorial, available online and on CDROM, produced as part of this contract. The tutorial covers erosion theory, data collection and evaluation, methodology, running the models using GIS, and interpreting results.

5. Fort Hood application

In the previous reports (Mitasova et al. 2000) we have applied the models to a predominately natural watershed at Fort Hood (Owl creek). Here we focus work on highly disturbed areas in the House Creek watershed. While the hydrology of this watershed has been investigated using various models, high resolution analysis of erosion and deposition by overland flow provides new insights about the distribution of sediment sources and their relation to land cover and topography. We obtained data from an NRCS erosion inventory for this area and entered them into our database. While the inventory data cannot be directly used for model calibration and validation because of the approach that was used, it provides some indication of the consistency of both the estimates of

input parameters, and erosion rates estimated in the field at a few locations and from the GIS data

GIS data.

5.1 Comparison with NRCS erosion inventory

The following is the database summary of 50 records with selected attributes observed at each inventory site which were entered into the GIS database. The original data were paper forms containing field measurements and observations for each inventory site. (Fort Hood data are courtesy Fred Schrank, NRCS).

```
SITES FILENAME: erosionf
_____
Header Information:
_____
                            erosion-house
          name
          description erosion inventory data for House creek at Ft. Hood
          labels X|Y|#ID|%K%L%S%LS%C%P%ET%EA%EG%AG%ER
Number of DIMENSIONS:
                                          2
_____
                      - - MIN - - - - MAX - -
          dim 1 604010.000000 613355.000000 Easting
          dim 2 3445785.000000 3452260.000000 Northing
Type of CATEGORY information: CELL_TYPE
_____
                      - - MIN - - - - MAX - -
                                            214 ID number
                                 158
Number of DOUBLE attributes: 11
_____

      - - MIN - -
      - - MAX - -

      dbl 1
      0.2
      0.39
      K-factor

      dbl 2
      40
      300
      Slope Leng

      dbl 3
      1
      14
      Slope ang

      dbl 4
      0.12
      1.45
      LS

      dbl 5
      0.003
      0.45
      C-factor

      dbl 6
      1
      1
      P-factor

      dbl 7
      0
      28

      dbl 8
      0
      13
      Soil loss

      dbl 9
      0
      89
      gully eros

      dbl 10
      0
      152
      road erosi

                      - - MIN - -
                                                     300 Slope Length [m]
                                                      14 Slope angle
                                                      13 Soil loss (USLE)(t/a/y)
89 gully erosion (t/y)
                                                                area gully affected (acre)
                                                     152 road erosion (t/y)
TOTAL SITES COUNTED: 50
_____
The inventory data is also available as a GRASS sites database file
(http://www.gis.uiuc.edu/erosion/finalreport/erosionf.txt).
```

Notes about the soil erosion inventory data :

• USDA inventory data are for 2 acre sites - usually 150-200m long while our results are for a reference point. We do not know where the reference point for each plot is located (center, top).

- Note that each plot is 50-70 cells long and 6-9 cells wide, so to really compare we would need to compute an estimate from all cells in that area, however we do not know how that area is oriented on the slope.
- Our upslope area is from the top of the drainage to the site; the observed slope length appears to be the length of the plot. (It should be measured from the top of the hill but it is not clear whether it really was).

X	Y	ID	K	dsd/L	S	LS1.1	LS1.4	LS1.6	LSVAR	С	ET	EA	EG	AG	ER
605462.	3451852	-	0.17	23	1.4dg	0.27	0.27	0.32	0.44	0.5	8/10		-		
605466	3451855	169	0.32	200	1.5	0.20	-	-	-	0.1	4	1.9	0	0	0
605725	3452206	-	0.17	14	1.9dg	0.30	0.39	0.45	0.40	0.1	2/2		+		
605721	3452202	160	0.32	200	3.5	0.46				0.1	9	4.3	24	0.2	32
605797	3452086		0.17	37	2.0dg	0.38	0.85	1.42	1.1	0.1	4/5		+		-
605799	3452086	162	0.32	150	4	0.47				0.2	17	8.2	39	0.5	3?
606091	3452263		0.17	17	1.5	0.23	0.32	0.40	0.35	0.1	2		-		-
606102	3452260	158	0.2	300	1.5	0.23				0.1	3	1.4	7	0.1	9
606121	3451954		0.17	20	2.3	0.43	0.67	0.88	0.7	0.5	14/17		-		-
606132	3451953	164	0.2	200	4	0.53				0.4	28	13	86	0.4	0
606220	3451780		0.28	27	1.2	0.17	0.26	0.34	0.32	0.01	0.2		+		
606232	3451784	171	0.32	200	3	0.35				0.2	13	6.3	1	0.1	0

• It is not clear what units are used for slope; ours is in degrees.





5.2 Planning prevention measures with GIS

From the point of view of conservation measures, contour filter strips, spreaders and, to some extent, grassed waterways, are effective in changing the turbulent flow typical for

rills and gullies to dispersed sheet flow. Erosion prevention in areas with sheet flow should focus on upper convex parts of the slope (that are prone to increased net erosion by creating accelerated flow). Dense vegetation should be preserved in these areas. Areas with more turbulent flow require flow dispersal measures and prevention of concentrated flow development which can cause severe and irreparable soil loss. Once concentrated flow fully develops it is more difficult to control erosion and more expensive control measures, such as sedimentation ponds, need to be added.

The first step in identifying erosion-prone areas is to select a numerical threshold from the results that identifies "hot spots", or areas to investigate for remediation (Figures 11, 12). Expert knowledge of the study area and field observations should be compared to values obtained by the model to help identify an appropriate threshold. Once a threshold value (or a series of priority values) is chosen, the hot spot areas are selected in the GIS. Appropriate vegetation may be added to the model in selected areas within the hotspots by changing the C-factor for those areas. The model run is then repeated and the results compared to those from the initial condition. Repeating this process and visualizing the results for multiple scenarios, using the GIS to analyze area, types, and cost of remediation, should help in the development of a satisfactory remediation plan (Figures 13, 14).







Figure 12. Hot spots from USPED



Figure 13. Current (dark green) and needed new (light green) protective cover based on RUSLE3d

sparse	cover
current	forest

%area acres
76.35|1253.40376|
7.73| 126.97239|

proposed new forest/dense cover 13.66 | 224.23337 |



Figure 14. Current (dark green) and needed new (light green) protective cover based on USPED.

	% area acres
sparse cover	79.58 1306.47097
current forest	6.94 113.91671
new dense vegetation	8.78 144.49688

Conclusions

The work summarized in this report provides a current application of state-of-the-art modeling of erosion and sediment transport deposition processes. Modeling has been improved by incorporating more accurate representations of physical processes such as soil detachment, and by the availability of higher resolution (and higher accuracy) data sources. Because of the lack of appropriate field data, however, validation and calibration of model parameters and results remains a research need.

The analysis of the RUSLE3D and USPED exponents explains how the flow term exponent controls the magnitudes and spatial pattern of detachment and net erosion/deposition. Because there are no extensive experimental data available to assign the values of this exponent based on local conditions several approaches can be taken for its determination. The most accurate results can be obtained if the exponent is calibrated using spatially distributed measurements. If no field observations are available, it is possible to assign a value to *m* based on the land cover, assuming that land cover has significant control over the type of flow. Other indicators of type of flow, such as surface roughness and soil properties can be used also. For many applications, especially where totals or averages are used, or the results are classified into a small number of classes, it is sufficient to use m=1.4. Because the range of values for slope is much smaller than the range of values for upslope area, the impact of its exponent on the results is smaller, but still significant so if the experimental data are available it is useful to include a range of values into calibration.

The tutorial developed as part of this effort provides a more complete discussion of work accomplished to date, as well as examples and instructions for application.

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